

Insights into Distributed Variational Inference for Bayesian Deep Learning

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Distributed Inference

- Motivations:
 - Training of complex models and large datasets needs a distributed implementation
 - Current distributed architectures are not efficient and do not scale well
 - Previous experimental studies only consider simple models
- Parameter-Server architecture with data-parallelism approach:
 - Data and workloads are distributed over worker nodes;
 - Parameter Server maintains globally shared parameters;



Experimental methodology

- Use mini-batch Stochastic gradient descent (SGD) algorithm
- Study the impact of design parameters:
 - Batch size
 - Learning rate
 - Number of Workers
 - Number of Parameter Servers
- Evaluate the performance through standard metrics:
 - Training time
 - Error Rate

Experimental Setup and Results

Fig. 1: Parameter-Server architecture

Synchronization schemes in TensorFlow implementation:



Stochastic Variational Inference for DGPs

- Stochastic Variational Inference
 - Intractable posterior over model parameters:

 $p(\boldsymbol{\theta}|\boldsymbol{Y},\boldsymbol{X}) = \frac{p(\boldsymbol{Y}|\boldsymbol{X},\boldsymbol{\theta})p(\boldsymbol{\theta})}{\int p(\boldsymbol{Y}|\boldsymbol{X},\boldsymbol{\theta})p(\boldsymbol{\theta})d\boldsymbol{\theta}};$

– Lower bound on marginal likelihood with mini-batch Stochastic Gradient optimization:

 $\log[n(Y|X|\theta)] > \frac{n}{2} \sum_{n \in \mathbb{N}} \sum_{n \in \mathbb{N}} \left[\log[n(\eta_{h}|\theta)]) - D_{VI}\left[n(\theta|X)\right]\right]$

Classification task;

E 0.9

0.8

0.

 log_{I0}

50

- MNIST dataset with 60000 samples;
- ▶ DGP model configuration: 2 hidden layers, 500 random features, 50 GPs in the hidden layers.



Batch size



Number of workers

$$\log[p(\mathbf{1} | \mathbf{\Lambda}, \mathbf{0})] \ge m \sum_{k \in \mathcal{I}_m} \operatorname{L}_q(\boldsymbol{\theta}) (\log[p(\boldsymbol{g}_k | \mathbf{0})]) = \operatorname{D}_{\mathrm{KL}}[q(\mathbf{0}) || p(\mathbf{0} | \mathbf{\Lambda})],$$

where $q(\theta)$ approximates $p(\theta|X)$;

– Estimate the expectation using Monte Carlo:

$$E_{q(\boldsymbol{\theta})}(\log[p(\boldsymbol{y}_k|\boldsymbol{\theta})]) \approx \frac{1}{N_{\rm MC}} \sum_{r=1}^{N_{\rm MC}} \log[p(\boldsymbol{y}_k|\tilde{\boldsymbol{\theta}}_r)] \quad \text{with} \quad \tilde{\boldsymbol{\theta}}_r \sim q(\boldsymbol{\theta});$$

- Deep Gaussian Processes (DGPs)
 - Deep probabilistic models;
 - Composition of functions:

 $\mathbf{f}(\mathbf{x}) = \left(\mathbf{h}^{(N_{\rm h}-1)} \left(\boldsymbol{\theta}^{(N_{\rm h}-1)}\right) \circ \ldots \circ \mathbf{h}^{(0)} \left(\boldsymbol{\theta}^{(0)}\right)\right) (\mathbf{x});$







 $\mathbf{h}^{(1)}\left(\mathbf{h}^{(0)}\left(\mathbf{x}\right)\right)$

Fig. 3: Illustration of how stochastic processes may be composed.

- ► DGPs with random feature expansions
 - Example of RBF kernel approximated with trigonometric functions:



Conclusions

Results of the experimental study:

- Large batch size and high learning rate:
 - improve Synchronous SGD convergence speed;
 increase model quality deterioration with Asynchronous SGD;

$\Phi_{\rm rbf} = \sqrt{\frac{\sigma^2}{N_{\rm RF}}} \left[\cos \left(F \Omega \right), \sin \left(F \Omega \right) \right],$

with

 $F = \Phi W$, $p(\Omega_{j}|\boldsymbol{\theta}) = \mathcal{N}(\mathbf{0}, \Lambda^{-1})$, $\Lambda = \operatorname{diag}(\boldsymbol{l}_{1}^{2}, \dots, \boldsymbol{l}_{d}^{2})$;

– DGPs become equivalent to Deep Neural Networks with low-rank weight matrices.



Fig. 4: Diagram of the proposed DGP model with random features.

- Scaling up the number of workers:
 - Asynchronous SGD reduces the training time, at expense of high error rate;
 - Synchronous SGD shows a smaller speed-up, but maintains low error rate;
- Scaling up the number of Parameter Servers:
 - can help to avoid bottlenecks at network level;
- produces negligible effects if the computation work prevails on the communication task; Future works:
 - Repeat the experiments with a different distributed setting;
 - ► Improve SGD distributed implementation, modifying the updates collection phase.

References

K. Cutajar, E. Bonilla, P. Michiardi, M. Filippone. *Random Feature Expansions for Deep Gaussian Processes*, ICML 2017.
 M. Abadi, P. Barham, J. Chen et al. *TensorFlow: A system for large-scale machine learning*, OSDI 2016.