

Robust Location-Aided Beam Alignment in mmWave Massive MIMO



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Beam Alignment in mmWave

- **Unfeasible** pilot, power and time resource **overhead** in Massive MIMO settings to establish communication
- One approach to reduce alignment overhead consists in **exploiting location information** [2, 3]
 - Possible acquisition through GNSSs, radars, ...
- **Noise** in the acquisition/estimation process
- **Unequal degrees** of information accuracies

Transmission Scenario

- Dual Massive MIMO setup
- Analog beamforming through codebooks \mathcal{V}_{TX} and \mathcal{V}_{RX}
- Pilot training over **small** subsets of the codebooks

Information Model

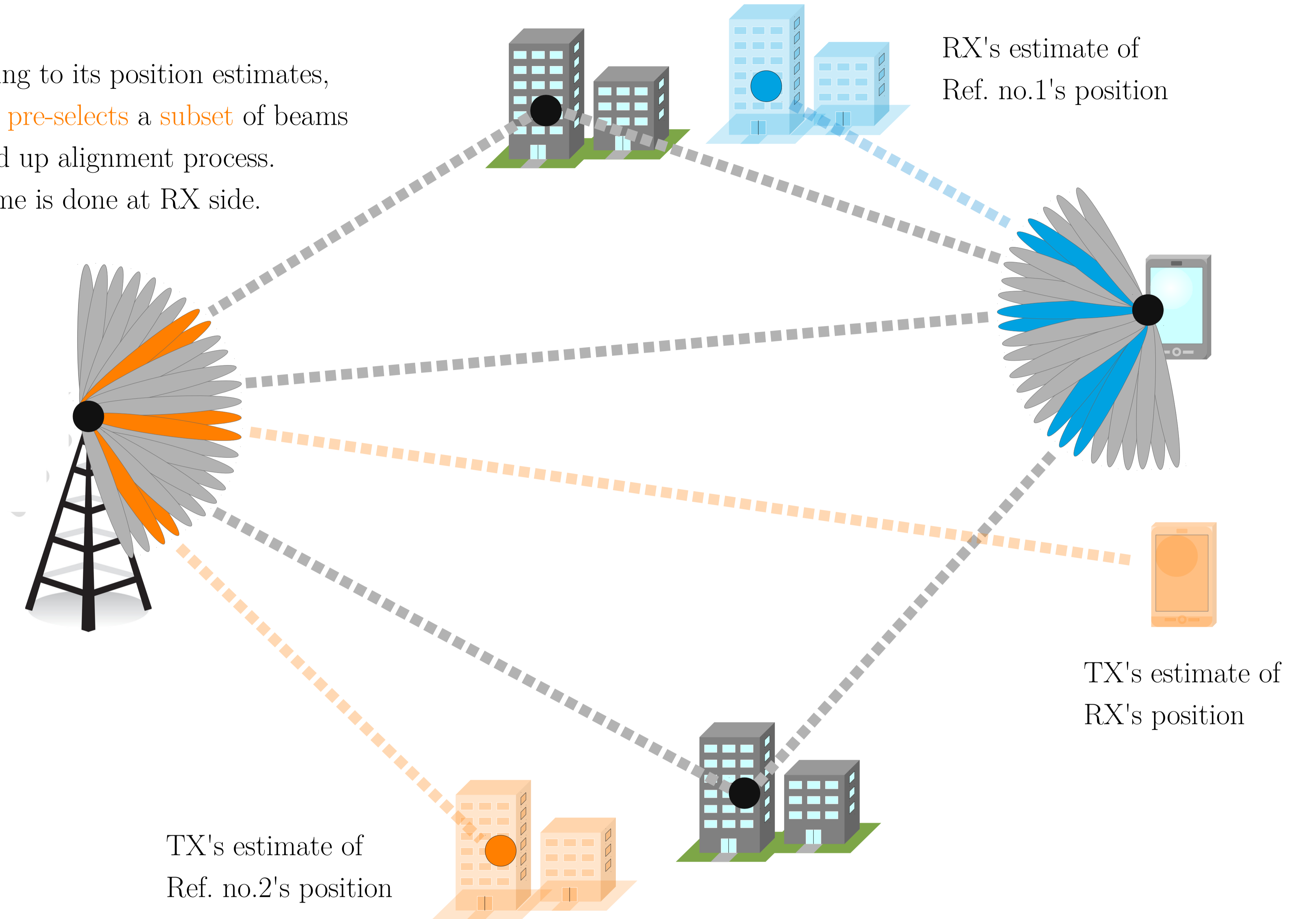
- **Distributed** model which emphasizes the decentralized nature of information available at TX and RX sides
- Position information at the **TX** and the **RX**:

$$\hat{\mathbf{P}}^{(TX)} = \mathbf{P} + \mathbf{E}^{(TX)}$$

$$\hat{\mathbf{P}}^{(RX)} = \mathbf{P} + \mathbf{E}^{(RX)}$$

- **Shared** statistical long-term information

According to its position estimates, the TX **pre-selects** a **subset** of beams to speed up alignment process. The same is done at RX side.



Coordinated Beam Alignment Methods

Goal: Design \mathcal{D}_{TX} and \mathcal{D}_{RX} , i.e. the sets of \mathcal{D}_{TX} and \mathcal{D}_{RX} pre-selected beams at the TX and the RX

- Figure of merit $\mathbb{E}[R(\mathcal{D}_{TX}, \mathcal{D}_{RX}, \mathbf{P})]$, where:

$$R(\mathcal{D}_{TX}, \mathcal{D}_{RX}, \mathbf{P}) = \max_{p \in \mathcal{D}_{TX}, q \in \mathcal{D}_{RX}} \log_2 \left(1 + \frac{G_{q,p}(\mathbf{P})}{N_0} \right)$$

Optimal Bayesian Beam Alignment

Decentralized beam pre-selection, based on **local** position information

- Beam pre-selection function at the TX and the RX:

$$d_{TX} : \mathbb{R}^{2 \times (L+1)} \rightarrow \mathcal{V}_{TX}$$

$$\hat{\mathbf{P}}^{(TX)} \mapsto d_{TX}(\hat{\mathbf{P}}^{(TX)})$$

$$d_{RX} : \mathbb{R}^{2 \times (L+1)} \rightarrow \mathcal{V}_{RX}$$

$$\hat{\mathbf{P}}^{(RX)} \mapsto d_{RX}(\hat{\mathbf{P}}^{(RX)})$$

→ Formulation as a **Team Decision** problem:

$$(d_{TX}^*, d_{RX}^*) = \underset{d_{TX}, d_{RX}}{\operatorname{argmax}} \mathbb{E}_{\mathbf{P}, \hat{\mathbf{P}}^{(TX)}, \hat{\mathbf{P}}^{(RX)}} \left[R(d_{TX}(\hat{\mathbf{P}}^{(TX)}), d_{RX}(\hat{\mathbf{P}}^{(RX)}), \mathbf{P}) \right]$$

- Functional Stochastic Optimization problem (notoriously difficult to solve, need for approximations)

2-Step Robust Beam Alignment

We first introduce the **Person-by-Person** (PbP) optimal, a **necessary** optimality condition for the optimal BA

- Each node takes the best strategy given the strategy at the other node

$$d_{TX}^{PP}(\hat{\mathbf{P}}^{(TX)}) = \underset{\mathcal{D}_{TX} \subset \mathcal{V}_{TX}}{\operatorname{argmax}} \mathbb{E}_{\mathbf{P}, \hat{\mathbf{P}}^{(RX)} | \hat{\mathbf{P}}^{(TX)}} \left[R(\mathcal{D}_{TX}, d_{RX}^{PP}(\hat{\mathbf{P}}^{(RX)}), \mathbf{P}) \right]$$

$$d_{RX}^{PP}(\hat{\mathbf{P}}^{(RX)}) = \underset{\mathcal{D}_{RX} \subset \mathcal{V}_{RX}}{\operatorname{argmax}} \mathbb{E}_{\mathbf{P}, \hat{\mathbf{P}}^{(TX)} | \hat{\mathbf{P}}^{(RX)}} \left[R(d_{TX}^{PP}(\hat{\mathbf{P}}^{(TX)}), \mathcal{D}_{RX}, \mathbf{P}) \right]$$

- (Still) Complicated solution due to the **interdependence** between the mappings d_{TX}^{PP} and d_{RX}^{PP}

Main idea: Approximate the PbP optimal beam alignment by **replacing** the PbP mapping inside the expectation operator with the **naive mapping** as described above

$$d_{TX}^{2-s}(\hat{\mathbf{P}}^{(TX)}) = \underset{\mathcal{D}_{TX} \subset \mathcal{V}_{TX}}{\operatorname{argmax}} \mathbb{E}_{\mathbf{P}, \hat{\mathbf{P}}^{(RX)} | \hat{\mathbf{P}}^{(TX)}} \left[R(\mathcal{D}_{TX}, d_{RX}^{1-s}(\hat{\mathbf{P}}^{(RX)}), \mathbf{P}) \right]$$

$$d_{RX}^{2-s}(\hat{\mathbf{P}}^{(RX)}) = \underset{\mathcal{D}_{RX} \subset \mathcal{V}_{RX}}{\operatorname{argmax}} \mathbb{E}_{\mathbf{P}, \hat{\mathbf{P}}^{(TX)} | \hat{\mathbf{P}}^{(RX)}} \left[R(d_{TX}^{1-s}(\hat{\mathbf{P}}^{(TX)}), \mathcal{D}_{RX}, \mathbf{P}) \right]$$

Naïve Beam Alignment

- TX and RX treat local information as **perfect** and **global**, i.e. it is **optimal** with perfect information

$$d_{TX}^{1-s}(\hat{\mathbf{P}}^{(TX)}) = \underset{\mathcal{D}_{TX} \subset \mathcal{V}_{TX}}{\operatorname{argmax}} \max_{\mathcal{D}_{RX} \subset \mathcal{V}_{RX}} R(\mathcal{D}_{TX}, \mathcal{D}_{RX}, \hat{\mathbf{P}}^{(TX)})$$

$$d_{RX}^{1-s}(\hat{\mathbf{P}}^{(RX)}) = \underset{\mathcal{D}_{RX} \subset \mathcal{V}_{RX}}{\operatorname{argmax}} \max_{\mathcal{D}_{TX} \subset \mathcal{V}_{TX}} R(\mathcal{D}_{TX}, \mathcal{D}_{RX}, \hat{\mathbf{P}}^{(RX)})$$
- **Misalignments** occur in case of imperfect information

Simulations

- $L=3$ dominant multipath components, of which 1 LoS
- 64 antennas (ULA), 64 beams in \mathcal{V}_{TX} and \mathcal{V}_{RX}
- Uniform bounded error model for location information

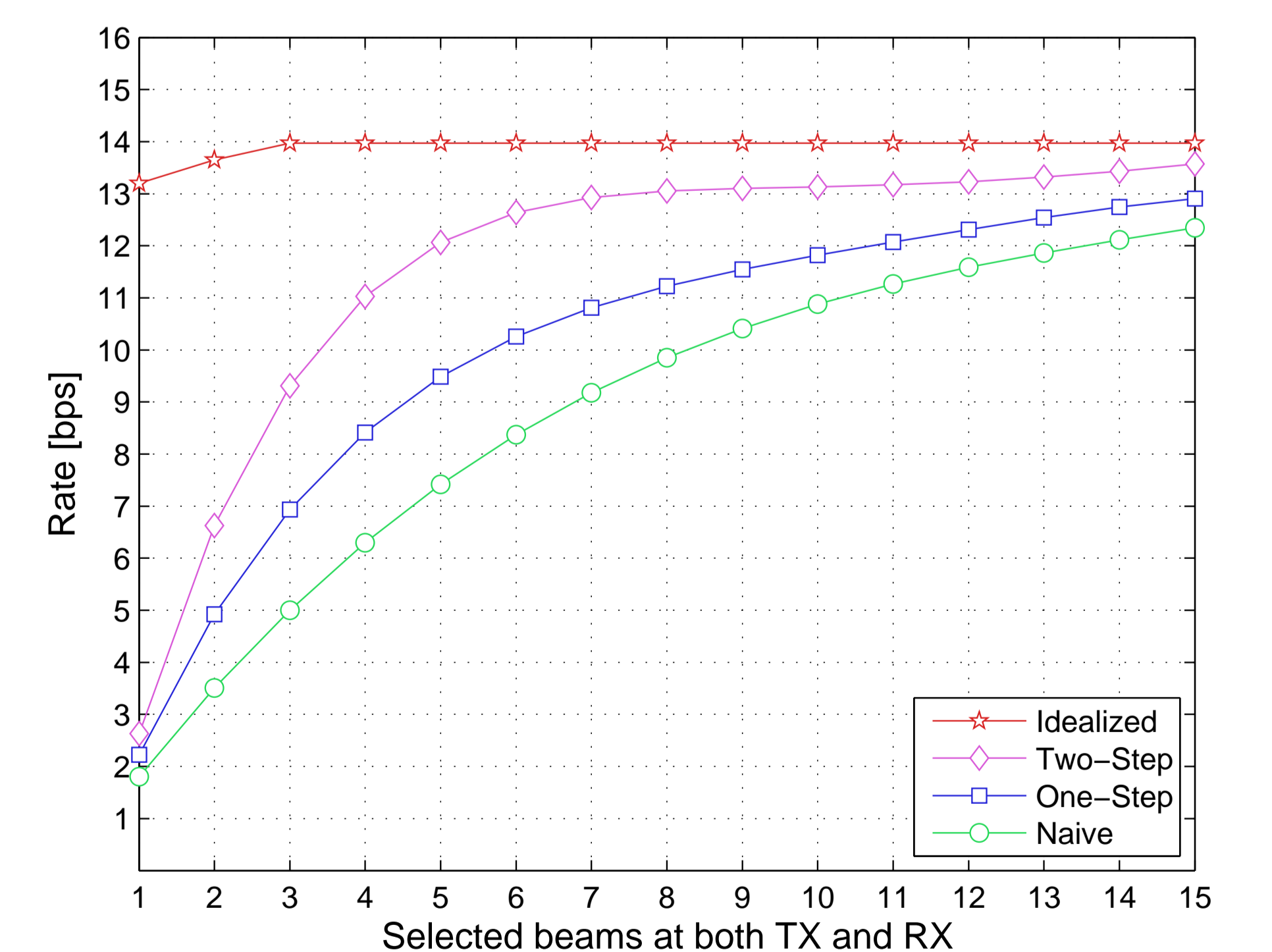


Figure 1: Rate vs # of selected beams at TX and RX, SNR = 10 dB.

References

- [1] F. Maschietti, D. Gesbert, P. de Kerret and H. Wymeersch, "Robust Location-Aided Beam Alignment in Millimeter Wave Massive MIMO", 2017. [Online: arxiv.org/abs/1705.01002]
- [2] N. Garcia, H. Wymeersch, E. G. Ström and D. Slock, "Location-Aided mmWave Channel Estimation for Vehicular Communication", IEEE SPAWC, 2016.
- [3] A. Ali, N. González-Prelcic, R. W. Heath, "Millimeter Wave Beam-Selection using Out-of-Band Spatial Information", 2017. [Online: arxiv.org/abs/1702.08574]